

# Misaligned Accretion: ADAFs, Slim Discs, QPOs and Jets

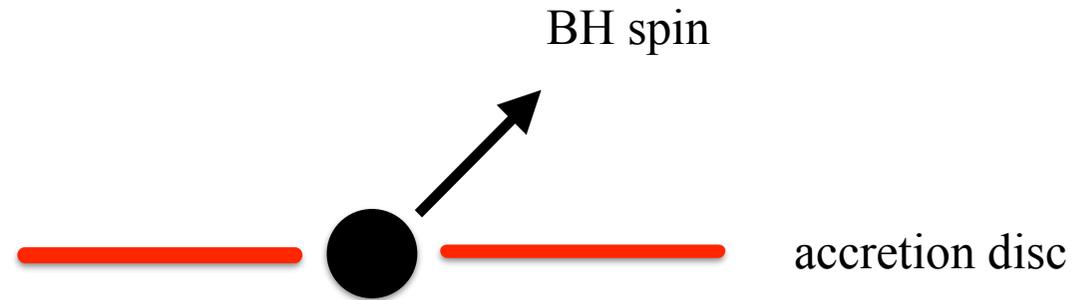


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Warsaw 2018

misalignment is **generic** for all accretion



obvious for AGN accretion - accretion plane set at large distance from SMBH

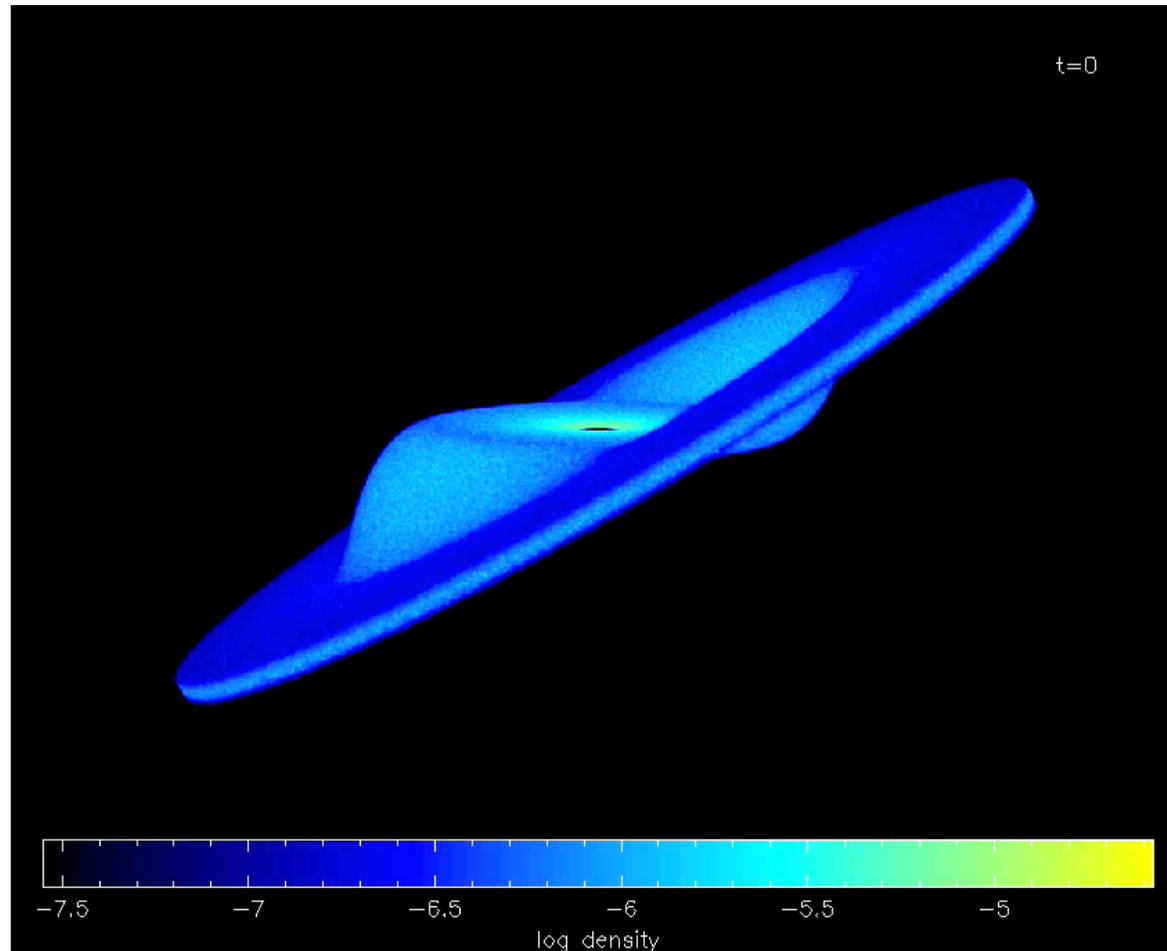
no good reason for alignment in high-mass X-ray binaries

even in low-mass X-ray binaries, accretion can only dilute misalignment after SN,  
but supplies too little angular momentum to remove it

**assuming alignment is a singular limit removing many effects**

# how does misaligned accretion proceed?

standard assumption: disc warps (Bardeen-Petterson)

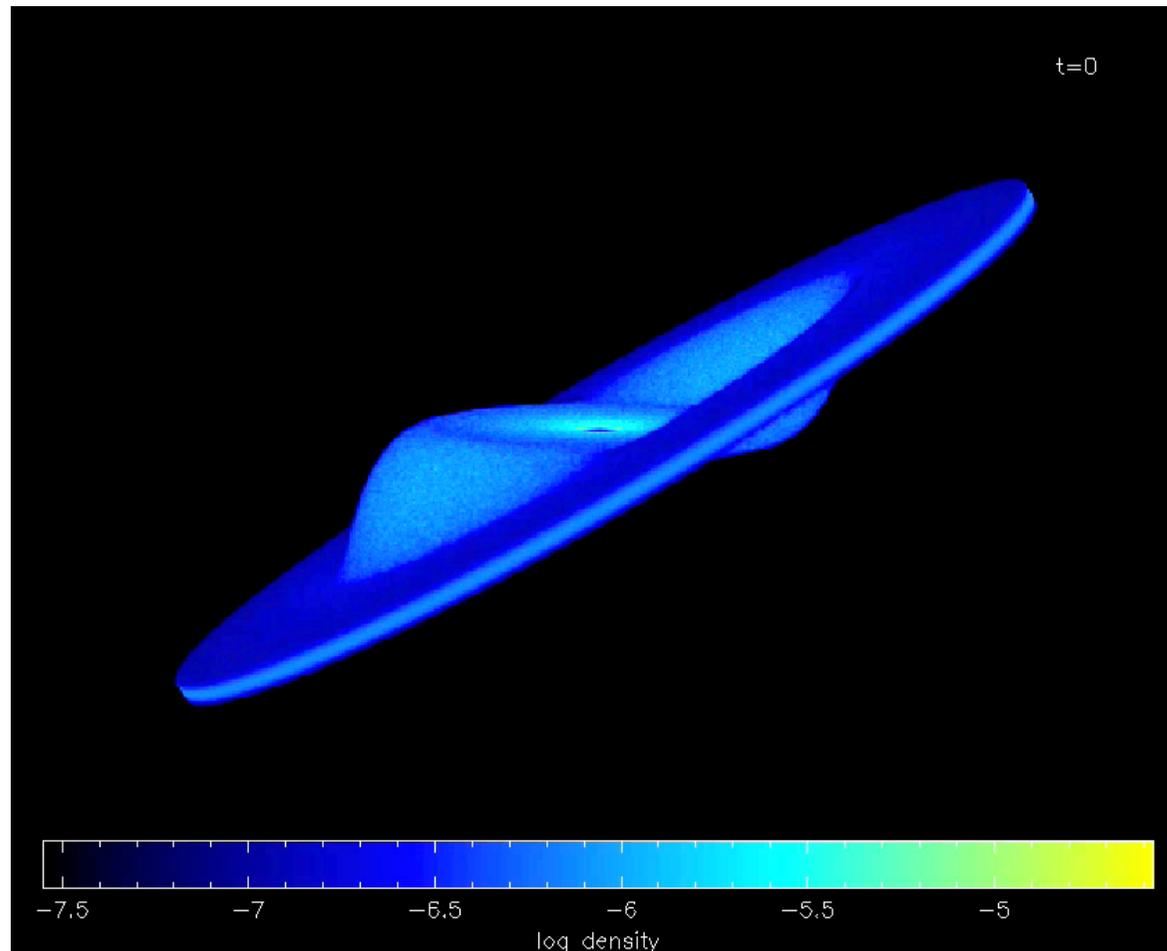


Lodato & Price, 2010

OK if inclination is moderate

## how does misaligned accretion proceed?

but if inclination is large, or viscosity weaker, **disc breaks!**



Lodato & Price, 2010

predicted by Papaloizou & Pringle, 1983; Ogilvie, 1999, 2000  
also recently found using GRMHD (Liska+, 2018)

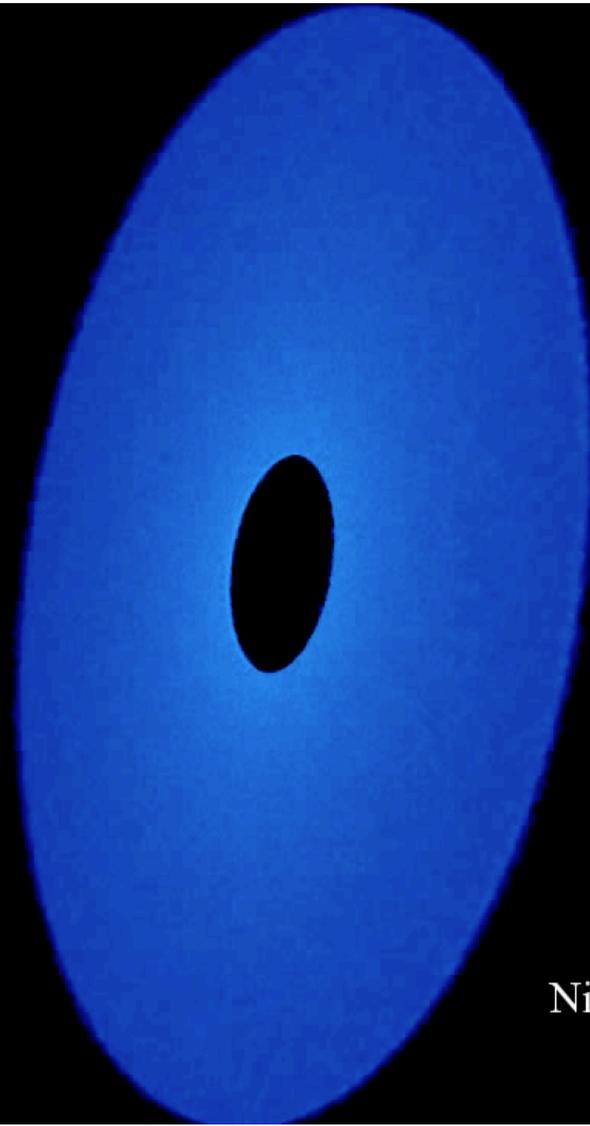
breaking can lead to tearing

broken parts of discs precess separately and interact

if they have precessed more than 180 degrees they are partially opposed

=> **INFALL**

*60 degree 3D*

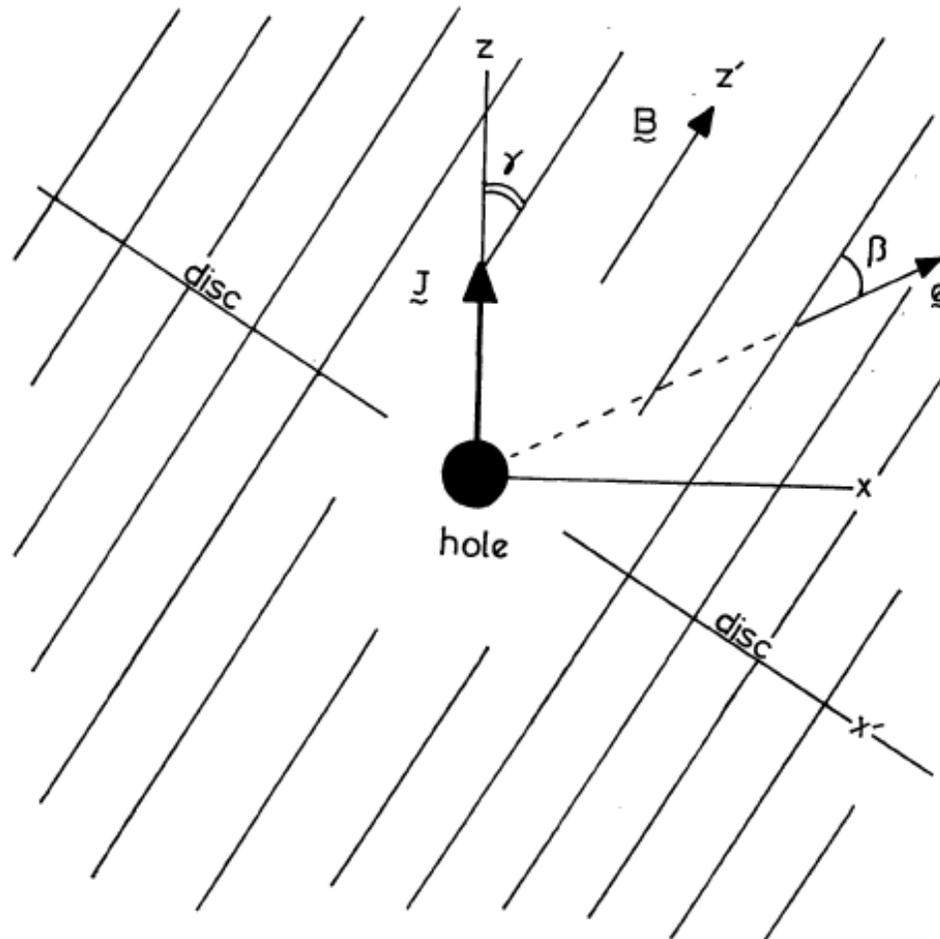


Nixon, King, Price & Frank (2012)

broken parts of discs precess separately and interact  
precession by more than 180 degrees => partially opposed => **infall**

could this make an ADAF?

misaligned accretion - BH spin inclined to external  
magnetic field (King & Lasota 1977)



**Fig. 1.** Black hole of angular momentum  $\vec{J}$  immersed in a magnetic field  $\vec{B}$  which becomes uniform far from the hole. The  $y$  and  $y'$  axes are identical and point into the paper, and  $\vec{e}$  is a radially pointing unit vector. Part of the disc considered in III of the text is shown in section (not to scale)

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aligns by **killing off the misaligned component** of  $\mathbf{J}$  while aligned component stays fixed:

$$J_{\parallel} = \text{constant}, \quad J_{\perp} = J_{\perp 0} e^{-t/t_h}, \text{ with}$$

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alignment utterly negligible except for very strong fields (GRBs?)

alignment torque extracts **energy** from hole spin

=> gravitational and EM **radiation**

if we set  $\boldsymbol{\mu} = R_g^3 \mathbf{B}$ ,  $\boldsymbol{\omega} = \mathbf{J} / M R_g^2$

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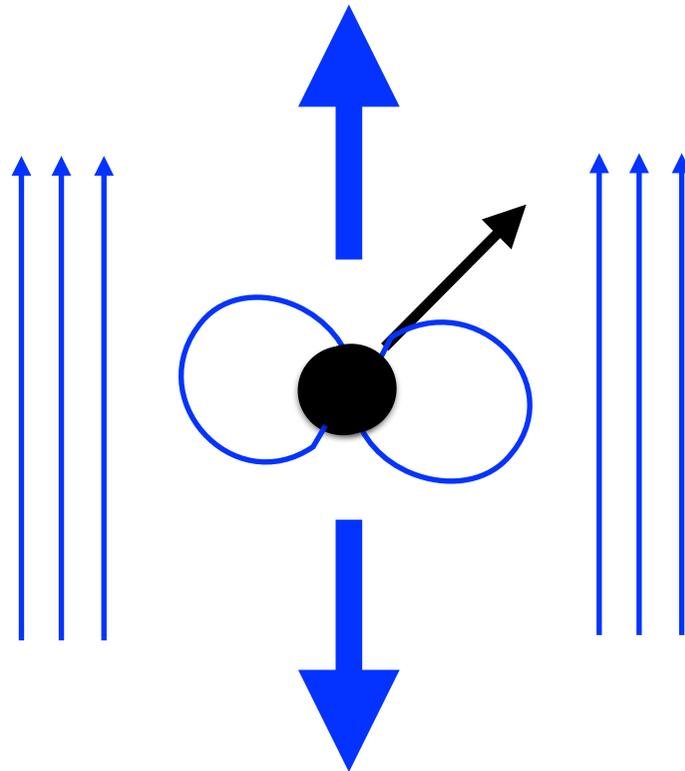
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**magnetic dipole radiation**

circular polarization carries off spin angular momentum

magnetic field induces a dipole near BH horizon  
this is forced to corotate inside the ergosphere

=> dipole radiation



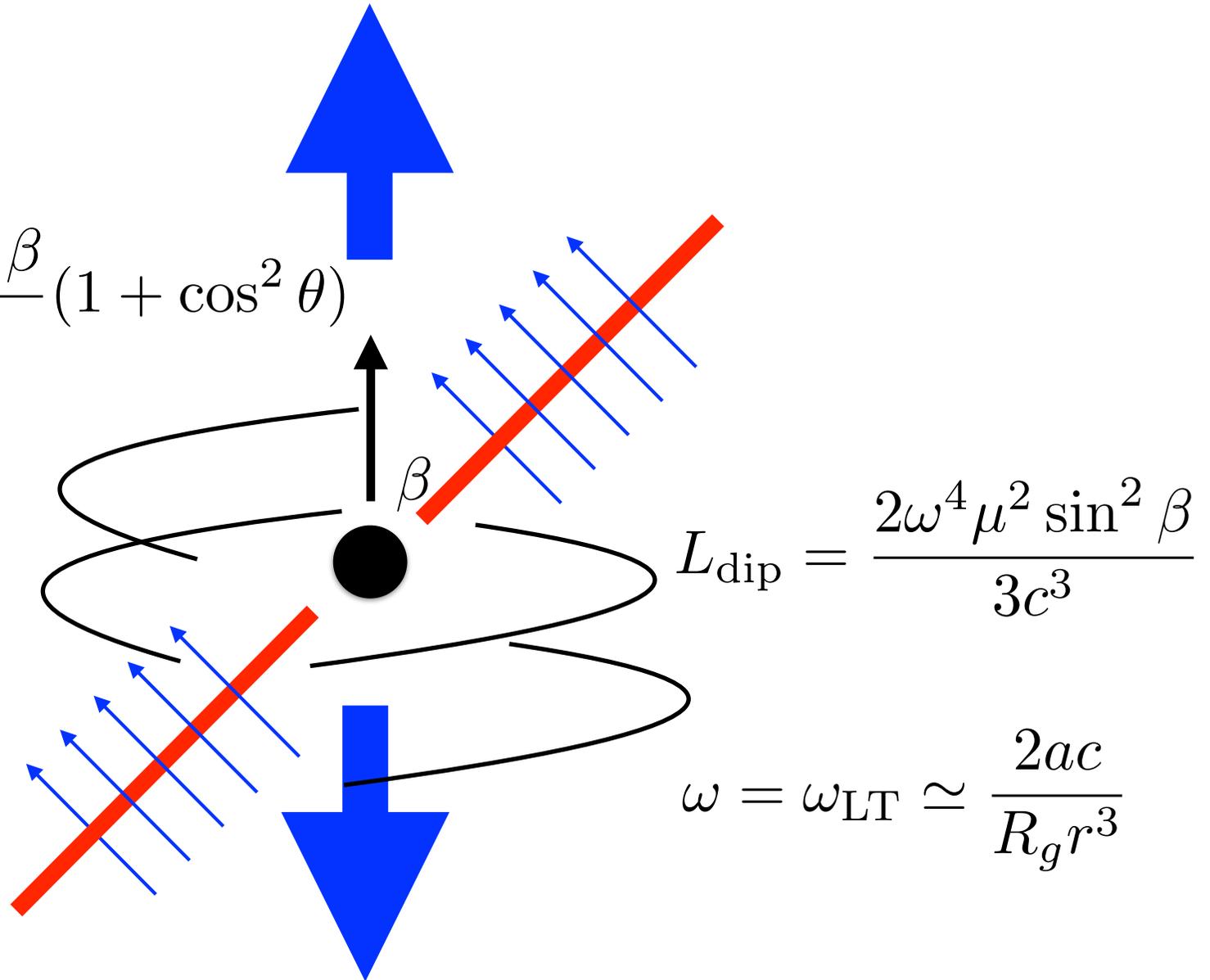
more interesting case - MRI field anchored in accretion disc rings: spin now fixed and **they** move: misalignment => **Lense-Thirring precession**

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$$\frac{dL_{\text{dip}}}{d\Omega} = \frac{\omega^4 \mu^2 \sin^2 \beta}{8\pi c^3} (1 + \cos^2 \theta)$$



$$L_{\text{dip}} = \frac{2\omega^4 \mu^2 \sin^2 \beta}{3c^3}$$

$$\omega = \omega_{\text{LT}} \simeq \frac{2ac}{R_g r^3}$$

King & Nixon  
ApJL 2018

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further:

this effect works *whatever* the nature of the accretor - if this is  
not a black hole, precession is driven by stellar quadrupole moment

dipole emission goes as  $\mu^2 \omega^4 \propto B^2 r^{-6}$  so dipole emission  
**sharply peaked towards disc inner edge** (ISCO for BH)

$$L_{\text{dip}} = \frac{128}{9\alpha} \left( \frac{R}{H} \right) \left( \frac{v_A}{c_s} \right)^2 \frac{\dot{M} c^2}{r^{17/2}} \left( 1 - \frac{1}{r^{1/2}} \right)^{11/20} a^4 \sin^2 \beta$$

$$\frac{L_{\text{dip}}}{L_{\text{acc}}} = \frac{128}{9\eta\alpha} \left( \frac{R}{H} \right) \left( \frac{v_A}{c_s} \right)^2 \frac{a^4 \sin^2 \beta}{r^{15/2}} \left( 1 - \frac{1}{r^{1/2}} \right)^{11/20}$$

$$r = R/R_g$$

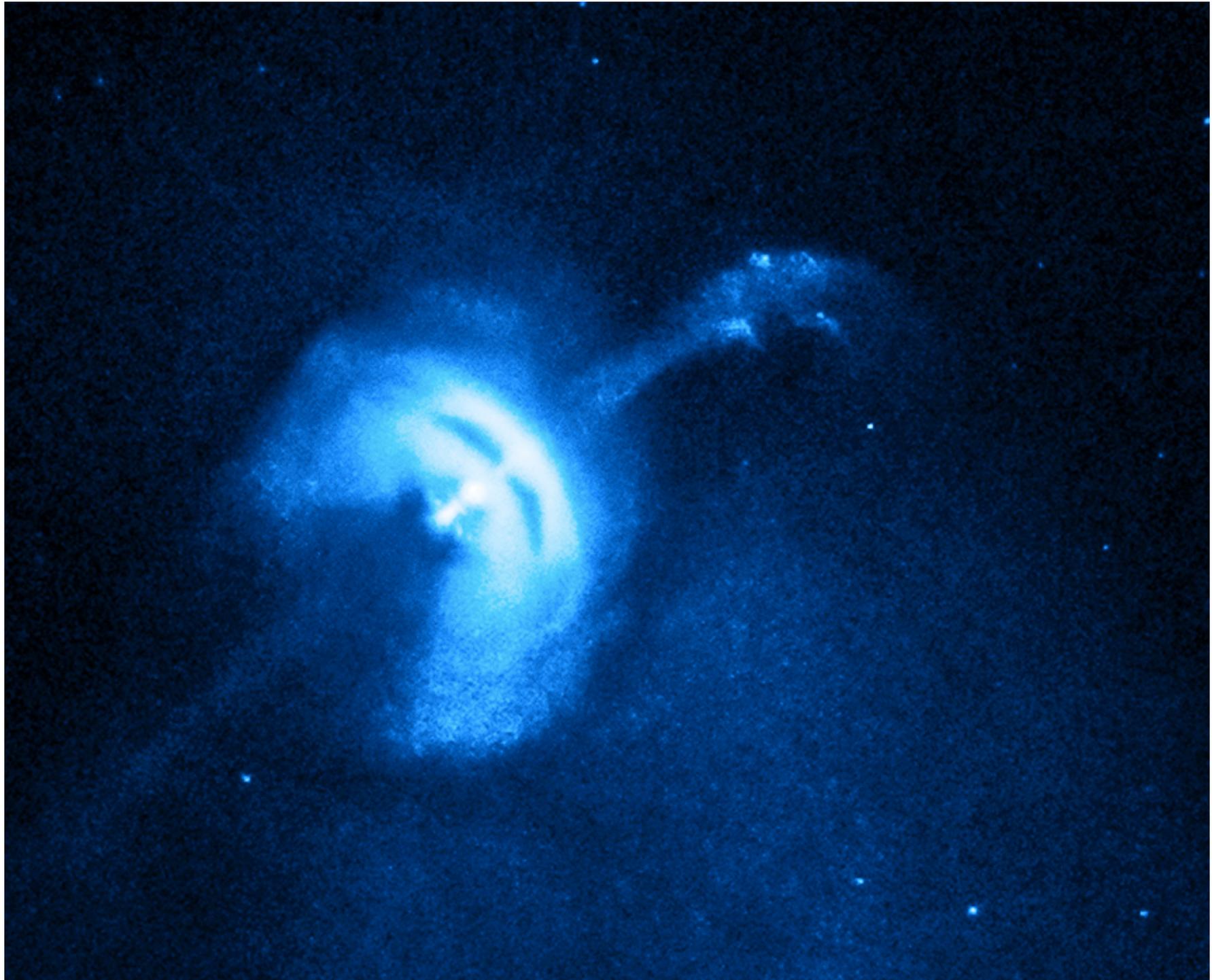
competition between alignment and accretion

emission is coherent at  $\omega < 2c/R_g \sim 4 \times 10^4$  Hz for  $10M_\odot$  black hole

so below plasma frequency, not directly observable

accretion/alignment competition  $\Rightarrow$  QPOs at  $\sim \omega$  (kHz)

as in radio pulsars, emission must drive outflow as jets along spin axis



# Summary

misaligned accretion + MRI =>

QPOs, and JETS along spin axis, for all accretors

MHD, GRMHD (even 'radiation' GRRMHD)

do **not** capture this, as displacement current set to zero:

no matter - radiation coupling