## Connecting Large Scale Structures

 to galactic spinChristophe Pichon
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Can we predict the spin of galaxies on the cosmic web from first principles?


## Outlinè

What is the geometry of spin near saddle?

- How do dark halo's spin flip relative to filament
- Why does it induce a transition mass: Efle, \& Lagrangiain theory? :


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- Why does it induce a transition mass: Efle in Lagrangian theory? . Why do we corre?
-Weak lensing
-AM stratification drives morphology
- Galaxy formation is not a ID manifold
- Because we,can understand something !


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Where' galaxies form does matter and can be traced back to ICs. Flattened filaments generate point-reflection-sivmetifo AM vorticity distribution: they induce the observed spin transition mass
dark halos don't form anywhere

$+$

Peak background split (PBS) in ID



## Does this anisotropic biassing have

a dynamical signature? yes! in term of spin!

Peak background split in 3D
without boost

# Does this anisotropic biassing have <br> a dynamical signature? yes! in term of spin! 

## Tidal Torque Theory in one cartoon

## Can we understand where spin and vorticity alignments come from?

-usual tidal torque theory

$$
L_{k}=\varepsilon_{i j k} I_{l i} T_{l j}
$$



YES! via conditional TTT subject to PBS

## Evidences of galaxy spin - filament alignment

## Cosmic Filament



See also:
Aragon-Calvo+ 2007, Hahn+ 2007, Paz+ 2008, Zhang+ 2009, Codis+ 20I2, Libeskind+ 20I3, Aragon-Calvo 20I3, Dubois+ 2014

## Evidences of galaxy spin - filament alignment

## Tempel+ (20|3) in the SDSS



See also:
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## Orientation of the spins w.r.t the filaments

Horizon 4Pi: DM only
$2 \mathrm{Gpc} / \mathrm{h}$ periodic box 4096³ DM part.
43 million dark halos at z=0
(Teyssier et al, 2009)

10000000 hrs CPU


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$$
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$$

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# Excess probability of alignment between the spins and their host filament 

## mass transition:

$$
\begin{gathered}
M_{\text {crit }}=4 \cdot 10^{12} M_{\odot} \\
M<M_{\text {crit }}: \text { aligned } \\
M>M_{\text {crit }}: \text { perpendicular }
\end{gathered}
$$

Excess probability of alignment between the spins and their host filament

(Codis et al, 2012)

How does the formation of the filaments generate spin parallel to them?

Voids/wall saddle repel...


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## Voids/wall saddle repel...

winding of walls into filaments


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Voids/wall saddle repel...
winding of walls into filaments

## Low-mass haloes: $\quad M<M_{\text {crit }}$



## High-mass haloes: $\quad M>M_{\text {crit }}$



## How do mergers along the filaments create spin perpendicular to them?

Halos catch up with each other along the filaments


## Explain transition mass?



## Explain transition mass?

Transition mass versus redshift: what's wrong???


## Tidal torque theory with a

 peak background split near a
## saddle



- The Idea
- walls/filament/peak locally bias differentially
tidal and inertia tensor: spin alignment reflect this in TTT
- The picture
- Geometry of spin near saddle: point reflection symmetric distribution, $1 / 10$ of 'naive size'
- The Maths
- Very simple ab initio prediction for mass transition

The Lagrangian view of spin/LSS connection

Can we understand where spin and vorticity alignments come from?
-usual tidal torque theory

$$
L_{k}=\varepsilon_{i j k} I_{l i} T_{l j}
$$


-anisotropy of the cosmic web: surrounding of a saddle point with typical geometry


## Tidal/Inertia mis-alignment


in saddle mid plane

## Tidal/Inertia mis-alignment


in saddle mid plane
spin wall -filament

spin filament-cluster
animation?

# Spin structure 

Flattened filament near Saddle

$$
L_{k}=\varepsilon_{i j k} I_{l i} T_{l j}
$$

$$
\approx \varepsilon_{i j k} H_{l i} T_{l j}
$$

Hessian

Tidal
Zeldovitch flow


Point reflection symmetry follows from 'spin one' property of spin!


## 3DTTT@ saddle?

- point reflection symmetric $\mathbf{r} \rightarrow-\mathbf{r}$ - vanish if no a-symmetry
perp. along $\mathrm{e}_{\varphi}$

Ispin // to filament
 perp =
along $\mathrm{e}_{\varphi}$
spatial transition+ ROI smaller

## Does it work with

 log-GaussianRandom Fields?

## point reflection symmetry for realistic sets of saddles from log GRF



Figure 11. Alignment of 'spin' along $\mathrm{e}_{z}$ in 2D as a function of quadrant rank, clockwise. As expected, from one quadrant to the next, the spin is flipping sign.

## Does it work with

 log-GaussianRandom Fields?
point reflection symmetry for realistic sets of saddles from log GRF


## Does it work with

## Dark matter @ z=0?

Clear predictions of aTTT


2D Spin acquisition near peaks

$$
L_{k}=\varepsilon_{i j k} I_{l i} T_{l j}
$$

filament
<L|peak> ${ }_{2 D}$ ?
Zeldovich flow
Theory will involve $2 p t$ correlation of field AND 2nd derivatives

## TTT@ saddle?

the Gaussain joint PDF of the derivatives of the field, $\mathbf{X}=\left\{x_{i j}, x_{i j k}, x_{i j k l}\right\}$ and $\mathbf{Y}=$ $\left\{y_{i j}, y_{i j k}, y_{i j k l}\right\}$ in two given locations ( $\mathbf{r}_{x}$ and $\mathbf{r}_{y}$ separated by a distance $r=\left|\mathbf{r}_{x}-\mathbf{r}_{y}\right|$ ) obeys

$$
\operatorname{PDF}(\mathbf{X}, \mathbf{Y})=\frac{1}{\operatorname{det}|2 \pi \mathbf{C}|^{1 / 2}} \times
$$

$$
\exp \left(-\frac{1}{2}\left[\begin{array}{l}
\mathbf{X}  \tag{A2}\\
\mathbf{Y}
\end{array}\right]^{\mathrm{T}} \cdot\left[\begin{array}{ll}
\mathbf{C}_{0} & \mathbf{C}_{\gamma} \\
\mathbf{C}_{\gamma}^{\mathrm{T}} & \mathbf{C}_{0}
\end{array}\right]^{-1} \cdot\left[\begin{array}{l}
\mathbf{X} \\
\mathbf{Y}
\end{array}\right]\right)
$$

subject to the "saddle" constraints (2D)
height

$$
\begin{aligned}
& x_{0,2}+x_{2,0}=\nu, x_{1,2}+x_{3,0}=0, x_{0,3}+x_{2,1}=0, \text { zero gradient } \\
& \kappa \cos (2 \theta)=\frac{1}{2}\left(x_{4,0}-x_{0,4}\right), \kappa \sin (2 \theta)=-x_{1,3}-x_{3,1}
\end{aligned}
$$

## TTT@ saddle?

the Gaussain joint PDF of the derivatives of the field, $\mathbf{X}=\left\{x_{i j}, x_{i j k}, x_{i j k l}\right\}$ and $\mathbf{Y}=$ $\left\{y_{i j}, y_{i j k}, y_{i j k l}\right\}$ in two given locations ( $\mathbf{r}_{x}$ and $\mathbf{r}_{y}$ separated by a distance $r=\left|\mathbf{r}_{x}-\mathbf{r}_{y}\right|$ ) obeys

$$
\exp \left(-\frac{1}{2}\left[\begin{array}{l}
\mathbf{X}  \tag{B4}\\
\mathbf{Y}
\end{array}\right]^{\mathrm{T}}\right.
$$

$$
\operatorname{PDF}\left(\mathbf{X}\left\{\begin{array}{l}
x_{0,0,2}+x_{0,2,0}+x_{2,0,0}=\nu, x_{1,0,2}+x_{1,2,0}+x_{3,0,0}=0, \\
x_{0,1,2}+x_{0,3,0}+x_{2,1,0}=0, x_{0,0,3}+x_{0,2,1}+x_{2,0,1}=0, \\
\kappa_{1,1}=\frac{1}{3}\left(x_{2,0,2}-x_{0,0,4}-2 x_{0,2,2}-x_{0,4,0}+x_{2,2,0}+2 x_{4,0,0}\right), \\
\kappa_{1,2}=x_{1,1,2}+x_{1,3,0}+x_{3,1,0}, \kappa_{1,3}=x_{1,0,3}+x_{1,2,1}+x_{3,0,1}, \\
\mathbf{Y}
\end{array}\right]^{\mathrm{T}} \cdot \begin{array}{l}
\kappa_{2,2}=\frac{1}{3}\left(x_{0,2,2}-x_{0,0,4}+2 x_{0,4,0}-2 x_{2,0,2}+x_{2,2,0}-x_{4,0,0}\right), \\
\kappa_{2,3}=x_{0,1,3}+x_{0,3,1}+x_{2,1,1} .
\end{array}\right.
$$

subject to the "saddle" constraints (2D)
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& x_{0,2}+x_{2,0}=\nu, x_{1,2}+x_{3,0}=0, x_{0,3}+x_{2,1}=0, \text { zero gradient } \\
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\end{aligned}
$$

Define the spin at point $\mathbf{r}_{y}$ along the $z$ direction as the anti-symmetric contraction of the de-traced tidal field and hessian:
(2D)

$$
\begin{gather*}
L\left(\mathbf{r}_{y}\right)=\varepsilon_{i j} \bar{y}_{i l} \bar{y}_{j m m l}=\left(y_{2,0}-y_{0,2}\right)\left(y_{1,3}+y_{3,1}\right)+ \\
\frac{y_{1,1}}{2}\left(y_{0,4}-y_{4,0}\right)-\frac{y_{1,1}}{2}\left(y_{4,0}-y_{0,4}\right) . \tag{A3}
\end{gather*}
$$

It is then fairly straightforward to compute the corresponding constrained expectation, $\langle L \mid \mathrm{pk}\rangle$, for $L$ as

$$
\begin{equation*}
L_{z}(r, \theta, \kappa, \nu)=\int L(\mathbf{Y}) \operatorname{PDF}(\mathbf{X}, \mathbf{Y} \mid \mathrm{pk}) \mathrm{d} \mathbf{X} \mathrm{~d} \mathbf{Y} \tag{A4}
\end{equation*}
$$

## e.g. for $\mathrm{n}=-2 \quad$ Incredibly simple prediction !

$$
L_{z}=\kappa \frac{r^{4} \sin (2 \theta)}{144} e^{-\frac{r^{2}}{2}}\left(\sqrt{6} \kappa\left(r^{2}-4\right) \cos (2 \theta)+6 \vee\right.
$$



2D Theory of Tidal Torque @ saddle?

$$
\delta\left(\mathbf{r}, \kappa, I_{1}, \nu \mid \mathrm{ext}\right)=\frac{I_{1}\left(\xi_{\phi \delta}^{\Delta \Delta}+\gamma \xi_{\phi \phi}^{\Delta \Delta}\right)+\nu\left(\xi_{\phi \phi}^{\Delta \Delta}+\gamma \xi_{\phi \delta}^{\Delta \Delta}\right)}{1-\gamma^{2}}+4\left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right) \xi_{\phi \delta}^{\Delta+}
$$



$$
f^{+}=\left(f_{11}-f_{22}\right) / 2 \text { and } f^{\times}=f_{12}
$$

## 2D Theory ofTidal Torque @ saddle?

$$
\left\langle L_{z} \mid \operatorname{ext}\right\rangle=L_{z}\left(\mathbf{r}, \kappa, I_{1}, \nu \mid \operatorname{ext}\right)=-16\left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \epsilon \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right)\left(L_{z}^{(1)}(r)+2\left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right) L_{z}^{(2)}(r)\right)
$$



$$
L_{z}^{(1)}(r)=\frac{\nu}{1-\gamma^{2}}\left[\left(\xi_{\phi \phi}^{\Delta+}+\gamma \xi_{\phi \delta}^{\Delta+}\right) \xi_{\delta \delta}^{\times \times}-\left(\xi_{\phi \delta}^{\Delta+}+\gamma \xi_{\delta \delta}^{\Delta+}\right) \xi_{\phi \delta}^{\times \times}\right]
$$

$$
L_{z}^{(2)}(r)=\left(\xi_{\phi x}^{\Delta \Delta} \xi_{\delta \delta}^{\times \times}-\xi_{\phi \delta}^{\times \times} \xi_{\delta \delta}^{\Delta \Delta}\right) \quad+\frac{I_{1}}{1-\gamma^{2}}\left[\left(\xi_{\phi \delta}^{\Delta+}+\gamma \xi_{\phi \phi}^{\Delta+}\right) \xi_{\delta \delta}^{\times \times}-\left(\xi_{\delta \delta}^{\Delta+}+\gamma \xi_{\phi \delta}^{\Delta+}\right) \xi_{\phi \delta}^{\times \times}\right]
$$

In order to compute the spin distribution, the formalism developed in Section 2 is easily extended to 3D. A critical (including saddle condition) point constraint is imposed. The resulting mean density field subject to that constraint becomes (in units of $\sigma_{2}$ ):

$$
\begin{equation*}
\delta\left(\mathbf{r}, \kappa, I_{1}, \nu \mid \mathrm{ext}\right)=\frac{I_{1}\left(\xi_{\phi \delta}^{\Delta \Delta}+\gamma \xi_{\phi \phi}^{\Delta \Delta}\right)}{1-\gamma^{2}}+\frac{\nu\left(\xi_{\phi \phi}^{\Delta \Delta}+\gamma \xi_{\phi \delta}^{\Delta \Delta}\right)}{1-\gamma^{2}}+\frac{15}{2}\left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right) \xi_{\phi \delta}^{\Delta+} \tag{3.1}
\end{equation*}
$$

where again $\overline{\mathbf{H}}$ is the detraced Hessian of the density and $\hat{\mathbf{r}}=\mathbf{r} / r$ and we define in 3D $\xi_{\phi x}^{\Delta+}$ as $\xi_{\phi \delta}^{\Delta+}=\left\langle\Delta \delta, \phi^{+}\right\rangle$, with $\phi^{+}=\phi_{11}-\left(\phi_{22}+\phi_{33}\right) / 2$. Note that $\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}$ is a scalar quantity defined explicitly as $\hat{r}_{i} \bar{H}_{i j} \hat{r}_{j}$. As in 2D, the expected spin can also be computed. In 3D, the spin is a vector, which components are given by $L_{i}=\varepsilon_{i j k} \delta_{k l} \phi_{l j}$, with $\boldsymbol{\epsilon}$ the rank 3 Levi Civita tensor. It is found to be orthogonal to the separation and can be written as the sum of two terms

$$
\begin{equation*}
\mathbf{L}\left(\mathbf{r}, \kappa, I_{1}, \nu \mid \text { ext }\right)=-15\left(\mathbf{L}^{(1)}(r)+\mathbf{L}^{(2)}(\mathbf{r})\right) \cdot\left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \boldsymbol{\epsilon} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right), \tag{3.2}
\end{equation*}
$$

where $\mathbf{L}^{(1)}$ depends on height, $\nu$, and on the trace of the Hessian $I_{1}$ but not on orientation

$$
\begin{aligned}
\mathbf{L}^{(1)}(r)= & \left(\frac{\nu}{1-\gamma^{2}}\left[\left(\xi_{\phi \phi}^{\Delta+}+\gamma \xi_{\phi \delta}^{\Delta+}\right) \xi_{\delta \delta}^{\times \times}-\left(\xi_{\phi \delta}^{\Delta+}+\gamma \xi_{\delta \delta}^{\Delta+}\right) \xi_{\phi \delta}^{\times \times}\right]\right. \\
& \left.+\frac{I_{1}}{1-\gamma^{2}}\left[\left(\xi_{\phi \delta}^{\Delta+}+\gamma \xi_{\phi \phi}^{\Delta+}\right) \xi_{\delta \delta}^{\times \times}-\left(\xi_{\delta \delta}^{\Delta+}+\gamma \xi_{\phi \delta}^{\Delta+}\right) \xi_{\phi \delta}^{\times \times}\right]\right) \mathbb{I}_{3}
\end{aligned}
$$

and $L^{(2)}(\mathbf{r})$ now depends on $\overline{\mathbf{H}}$ and on orientation:

$$
\begin{aligned}
\mathbf{L}^{(2)}(\mathbf{r})=-\frac{5}{8}\left[2 \left(\left(\xi_{\phi \delta}^{\Delta+}\right.\right.\right. & \left.\left.-\xi_{\phi \delta}^{\Delta \Delta}\right) \xi_{\delta \delta}^{\times \times}-\left(\xi_{\delta \delta}^{\Delta+}-\xi_{\delta \delta}^{\Delta \Delta}\right) \xi_{\phi \delta}^{\times \times}\right) \overline{\mathbf{H}} \\
& \left.+\left(\left(7 \xi_{\delta \delta}^{\Delta \Delta}+5 \xi_{\delta \delta}^{\Delta+}\right) \xi_{\phi \delta}^{\times \times}-\left(7 \xi_{\phi \delta}^{\Delta \Delta}+5 \xi_{\phi \delta}^{\Delta+}\right) \xi_{\delta \delta}^{\times \times}\right)\left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right) \mathbb{I}_{3}\right]
\end{aligned}
$$

# 3D Transition mass? 

Lagrangian theory capture spin flip !

Transition mass associated with size of quadrant


# 3D Transition mass? 

Lagrangian theory capture spin flip !

Transition mass associated with size of quadrant


## Geometry of the saddle provides a natural 'metric' (local frame as defined by Hessian @ saddle) relative to which <br> Cloud in dynamical evolution of DH is predicted.

 cloud effect

Figure 5. Left: logarithmic cross section of $M_{p}(r, z)$ along the most likely (vertical) filament (in units of $\left.10^{12} M_{\odot}\right)$. Right: corresponding cross section of $\langle\cos \hat{\theta}\rangle(r, z)$. The mass of halos increases towards the nodes, while the spin flips.

## geometric split

mass split

Geometry of the saddle provides a natural 'metric' (local frame as defined by Hessian @ saddle) relative to which

Cloud in dynamical evolution of DH is predicted.
cloud effect


Figure 6. Mean alignment between spin and filament as a function of mass for a filament smoothing scale of $5 \mathrm{Mpc} / h$. The spin flip transition mass is around $410^{12} M_{\odot}$.
geometric split
mass split

## Link with Eulerian vorticity?

## density caustic

AM Lagragian map


Figure 5. top: Density caustic; Bottom: Zeldovitch mapping of the spin distribution

## Link with Eulerian vorticity?

## density caustic

Figure 5. tor
1 mapping of the spin distri -2

## Back to wall winding: generation of vorticily

## Alignement of vorkicity with cosmic web


$\underbrace{Y}_{2} x$

## braids structure of vorticity.

## Growth of large-scale structure

In the initial phase of structure formation, flows are laminar and curl-free.
This is no longer valid at the shell-crossing.

Thin slice of a $D M$ simulation at $z=0$.


## Vorticity generation

In the initial phase of structure formation, flows are laminar and curl-free.
This is no longer valid at the shell-crossing.

Thin slice of a $D M$ simulation at $z=0$.


## Vorticity is generated and is confined in the filaments.



## Alignment of vorticity with filaments

## Vorticity is aligned with the filaments.



Cosmid Filament

Filaments and walls are identified with DISPERSE: Sousbie+ (2011).

## Geometry of the vorticity cross-section



Pichon \& Bernardeau (1999)


## Cross-sections are typically divided in 4 quadrants.

Theoretical prediction from Pichon \& Bernardeau 1999

Low-mass halos are aligned with the filament


- Mhalo < Mcrit alignment of halo spin with filament increases with mass.
- Mcrit


High-mass halos are perpendicular


- Mcrit
- Mhalo > Mcrit halo spin tends to be perpendicular to the filament.

Mass dependent Halo spin - filament alignment

- Mhalo < Mcrit $\left.N^{n} \boldsymbol{n}^{2}\right\rangle$
 alignment of halo spin
with filament increases alignment of halo spin
with filament increases with mass.
- Mcrit
- Mhalo > Mcrit halo spin tends to be halo spin tends to be filament.


Halo-spin vorticity alignment


## Geometry of the vorticity cross-section

Stacked profile


Pichon \& Bernardeau (1999)




High vorticity regions are located at the edges of the filament.

## Mass transition for spin alignment

Idealized toy model: The position is fixed and the radius of the halo increases:



## Transition mass is correlated with the size of the quadrants.

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## Mass transition for spin alignment

Idealized toy model: The position is fixed and the radius of the halo increases:



## Transition mass is correlated with the size of the quadrants.

## in short...

Vorticity is confined in the filaments, and aligned with them. The cross-section with a plane perpendicular to the filament is typically quadripolar.

*) Halo spins are aligned with the same polarity than vorticity in quadrants.

Qualitatively, the transition mass in the alignment could be correlated with the size of the quadrant.


## Explain transition mass? YES!

Transition mass versus redshift

horizon $4 \pi$
skeleton of LSS

Only 2 ingredients: a) spin is spin one b) filaments flattened

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Transition mass versus redshift

horizon $4 \pi$
skeleton of LSS

Only 2 ingredients: a) spin is spin one b) filaments flattened

Outer halo

Filament

## Connecting Eulerian \&

 Lagrangian theoriesOuter halo

## +Zeldovitch boost

BUT in // from the pt of view of LSS


Complementary vorticity advection view

## Take home message...

- Morphology (= AM stratification) driven by LSS in cosmic web: it explains Es \& Sps where, how \& why from ICs
- Signature in correlation between spin and internal kinematic structure of cosmic web on larger scales.
- Process driven by simple PBS/biassed clustering dynamics:
- requires updating TTT to saddles: simple theory :-)
- can be expressed into an Eulerian theory via vorticity

Where galaxies form does matter, and can be traced back to ICs Flattened filaments generate point-reflection-symmetric AM/vorticity distribution: they induce the observed spin transition mass

- which is why the $\delta$-Web is the best :-)


## What about galaxies ??

- Horizon-AGN simulation Jade (CINES)
(PI Y. Dubois, Co-I J. Devriendt \& C. Pichon)
- $\mathrm{L}_{\text {box }}=100 \mathrm{Mpc} / \mathrm{h}$
- $1024^{3}$ DM particles $M_{D M, r e s}=8 \times 10^{7} M_{\text {sun }}$
- Finest cell resolution $\mathrm{dx}=1 \mathrm{kpc}$
- Gas cooling \& UV background heating
- Low efficiency star formation
- Stellar winds + SNII + SNIa
- O, Fe, C, N, Si, Mg, H
- AGN feedback radio/quasar
- Outputs
(backed up and analyzed on BEYOND)
- Simulation outputs
- Lightcones $\left(1^{\circ} \times 1^{\circ}\right)$ performed on-the-fly
- Dark Matter (position, velocity)
- Gas (position, density, velocity, pressure, chemistry)
- Stars (position, mass, velocity, age, chemistry)
- Black holes (position, mass, velocity, accretion rate)
- $z=1.5$ using 3 Mhours on 4096 cores
horizon-AGN.projet-horizon.fr
$z=1.2$


## Part V Outline

- Can morphology/physics trace spin flip?
- Are transition masses consistent?
- The fate of forming galaxies
- The fate of merging galaxies


## Galaxies versus dense filaments



# can morphology trace spin flip? 

- thanks to AGN feedback we have morphological diversity


Filament-galactic spin \& mass


## Can morphological/physical properties of galaxies trace spin flip?



## is morphometric transition mass

 consistent with DM ?
## Final point 1/2: low mass galaxies

What is the physical origin of low mass galaxies spin-filament alignment?
Vorticity arising from kin. structure of filament!



## Final point 2/2: high mass galaxies

What is the physical origin of spin flip? high mass galaxies merge!


## Transition mass versus merging rate <br> for galaxies

PDF of $\mu$ over 4 timesteps $\delta t$

## SMOOTH ACCRETION

- Gas inflows (re)-align galaxies with their filament

no merger : orientation versus look-back time


Caught in the rhythm: satellites in their galactic plane
C. Welker ${ }^{1 \star}$, Y. Dubois ${ }^{1}$, C. Pichon ${ }^{1,2}$, J. Devriendt ${ }^{3,4}$ and N. E. Chisari ${ }^{3}$ filament


## Are the imprints of LSS noticeable on galaxy properties ?



1D level crossing primer


$$
\left.\begin{array}{rl}
n_{\nabla \rho} \mathrm{dx} & =\mathcal{P}(\rho=0 \mid \nabla \rho) \mathrm{d} \rho \\
\mathrm{~d} \rho & =-\nabla \rho \mathrm{dx}
\end{array}\right\} \Rightarrow n_{\nabla \rho}=\mathcal{P}(\rho=0 \mid \nabla \rho)|\nabla \rho|
$$

$$
n_{\text {zeroes }}=\int_{\substack{-\infty \\ \infty}}^{\infty} \mathrm{d} \nabla \rho|\nabla \rho| \mathcal{P}(\rho=0, \nabla \rho) \propto \frac{\sigma_{1}}{\sigma_{0}}
$$

$$
n_{\text {extrem }}=\int_{-\infty} \mathrm{d} \nabla \nabla \rho|\nabla \nabla \rho| \mathcal{P}(\nabla \rho=0, \nabla \nabla \rho) \propto \frac{\sigma_{2}}{\sigma_{1}}
$$

## Summary of 1D Gaussian calculations

Fundamental scales $R_{0}, R_{*}$

$$
\begin{aligned}
& n_{\text {zero }} \propto \frac{1}{R_{0}}=\frac{\sigma_{1}}{\sigma_{0}}, \quad n_{\text {maxima }} \propto \frac{1}{R_{*}}=\frac{\sigma_{2}}{\sigma_{1}} \\
& \frac{n_{\text {maxima }}}{n_{\text {zero }}}=\gamma \equiv \frac{\sigma_{1}^{2}}{\sigma_{0} \sigma_{2}}=\frac{R_{*}}{R_{0}}, \quad \gamma \in[0,1]
\end{aligned}
$$

More sophisticated result:
Maxima above threshold $\eta=\rho / \sigma_{0}$


$$
n_{\max }\left(\rho>\eta \sigma_{0}\right)= \begin{cases}n_{\max } \mathcal{P}(\eta) & \gamma \rightarrow 0 \\ n_{\max } \mathcal{P}(\eta)(\gamma \eta) & \gamma \rightarrow 1\end{cases}
$$

## back to 2D Theory

## without Hessian approximation

$$
\begin{gathered}
L_{k}=\varepsilon_{i j k} I_{l i} T_{l j} \\
\quad \approx \varepsilon_{i j n \pi} \frac{I T l i}{} T_{l j} \\
\text { Hessian }
\end{gathered}
$$



