Connecting Large Scale Structures to galactic spin

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Can we predict the spin of galaxies on the cosmic web from first principles?

MareNostrum z=1.55



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Outline

What is the geometry of spin near saddle?
How do dark halo's spin flip relative to filament
Why does it induce a transition mass: Lifering & Lagrangian theory?

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• What is the geometry of spin near saddle? • How do dark halo's spin flip relative to filament • Why does it induce a transition mass: Eulerian & Lagrangian theory? Why do we care? •Weak lensing AM stratification drives morphology Galaxy formation is not a ID manifold • Because we can understand something !

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• What is the geometry of spin near saddle? • How do dark halo's spin flip relative to filament • Why does it induce a transition mass: Eulerian & Lagrangian theory? Why do we care? •Weak lensing AM stratification drives morphology Galaxy formation is not a ID manifold • Because we can understand something !

Where galaxies form does matter, and can be traced back to ICs. Flattened filaments generate point-reflection-symmetric AM/vorticity distribution: they induce the observed spin transition mass



Peak background split in 3D

 \odot

with

boost



Does this anisotropic biassing have a dynamical signature? yes! in term of spin!

Peak background split in 3D



Does this anisotropic biassing have a dynamical signature? yes! in term of spin!

Tidal Torque Theory in one cartoon

Can we understand where spin and vorticity alignments come from?

-usual tidal torque theory

$$L_k = \varepsilon_{ijk} \, I_{li} \, T_{lj}$$

Et Voilà !

tidal tensor T_{ij} Zeldovich boost inertia tensor of halo I_{ij}

YES! via conditional TTT subject to PBS

"Cond' prob, good stuff!"

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Evidences of galaxy spin - filament alignment

Cosmic Filament



See also:

Aragon-Calvo+ 2007, Hahn+ 2007, Paz+ 2008, Zhang+ 2009, Codis+ 2012, Libeskind+ 2013, Aragon-Calvo 2013, Dubois+ 2014

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Evidences of galaxy spin - filament alignment



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Orientation of the spins w.r.t the filaments

Horizon 4Pi:

DM only 2 Gpc/h periodic box 4096³ DM part. 43 million dark halos at z=0

(Teyssier et al, 2009)

10 000 000 hrs CPU



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Excess probability of alignment between the spins and their host filament

mass transition:

 $M_{\rm crit} = 4 \cdot 10^{12} M_{\odot}$

 $M < M_{\rm crit}$: aligned

 $M > M_{\rm crit}$: perpendicular



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How does the formation of the filaments generate spin parallel to them?

Voids/wall saddle repel...



How does the formation of the filaments generate spin parallel to them?



Voids/wall saddle repel...

winding of walls into filaments

How does the formation of the filaments generate spin parallel to them?



Low-mass haloes: $M < M_{crit}$



redshift

High-mass haloes: $M > M_{crit}$



 $M_{\rm crit} = 4 \cdot 10^{12} M_{\odot}$

formed at low z by mergers inside the filaments



How do mergers along the filaments create spin perpendicular to them?



Explain transition mass?





Explain transition mass?

Transition mass versus redshift: wrong???



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Tidal torque theory with a peak background split near a **saddle**



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The Idea

walls/filament/peak locally bias differentially tidal and inertia tensor: spin alignment reflect this in TTT

The picture

Geometry of spin near saddle: point reflection symmetric distribution, 1/10 of 'naive size'

The Maths

Server Simple ab initio prediction for mass transition

The Lagrangian view of spin/LSS connection

Can we understand where spin and vorticity alignments come from?



-anisotropy of the cosmic web: surrounding of a saddle point with typical geometry



Tidal/Inertia mis-alignment



Tidal/Inertia mis-alignment



spin wall -filament



Spin structure Flattened filament AM vectors near Saddle $L_k = \varepsilon_{ijk} I_{li} T_{lj}$ $\approx \varepsilon_{ijk} H_{li} T_{lj}$ Hessian Zeldovitch flow Tida







Does it work with log-Gaussian Random Fields?

point reflection symmetry for realistic sets of saddles from log GRF



Figure 11. Alignment of 'spin' along e_z in 2D as a function of quadrant rank, clockwise. As expected, from one quadrant to the next, the spin is flipping sign.

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Does it work with log-Gaussian Random Fields?

point reflection symmetry for realistic sets of saddles from log GRF



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2D Spin acquisition near peaks

Codis, Pichon, Pogosyan, in prep.



TT@ saddle?

the Gaussain joint PDF of the derivatives of the field, $\mathbf{X} = \{x_{ij}, x_{ijk}, x_{ijkl}\}$ and $\mathbf{Y} = \{y_{ij}, y_{ijk}, y_{ijkl}\}$ in two given locations (\mathbf{r}_x and \mathbf{r}_y separated by a distance $r = |\mathbf{r}_x - \mathbf{r}_y|$) obeys

$$ext{PDF}(\mathbf{X},\mathbf{Y}) = rac{1}{ ext{det}|2\pi\mathbf{C}|^{1/2}} imes$$

$$\exp\left(-\frac{1}{2}\begin{bmatrix}\mathbf{X}\\\mathbf{Y}\end{bmatrix}^{\mathrm{T}}\cdot\begin{bmatrix}\mathbf{C}_{0}&\mathbf{C}_{\gamma}\\\mathbf{C}_{\gamma}^{\mathrm{T}}&\mathbf{C}_{0}\end{bmatrix}^{-1}\cdot\begin{bmatrix}\mathbf{X}\\\mathbf{Y}\end{bmatrix}\right),\quad(A2)$$
subject to the "saddle" constraints (2D)
$$\overset{\text{height}}{x_{0,2}+x_{2,0}}=\nu,\ x_{1,2}+x_{3,0}=0,\ x_{0,3}+x_{2,1}=0,\ ^{\text{zero gradient}}$$

$$\kappa\cos(2\theta)=\frac{1}{2}\left(x_{4,0}-x_{0,4}\right),\ \kappa\sin(2\theta)=-x_{1,3}-x_{3,1}.$$

$$\overset{\text{parametrized curvature}}{x_{0,2}+x_{2,0}}$$

TT@ saddle?

the Gaussain joint PDF of the derivatives of the field, $\mathbf{X} = \{x_{ij}, x_{ijk}, x_{ijkl}\}$ and $\mathbf{Y} = \{y_{ij}, y_{ijk}, y_{ijkl}\}$ in two given locations (\mathbf{r}_x and \mathbf{r}_y separated by a distance $r = |\mathbf{r}_x - \mathbf{r}_y|$) obeys

$$PDF(\mathbf{X} \left\{ \begin{array}{c} x_{0,0,2} + x_{0,2,0} + x_{2,0,0} = \nu, \ x_{1,0,2} + x_{1,2,0} + x_{3,0,0} = 0, \ \mathbf{X}_{0,1,2} + x_{0,3,0} + x_{2,1,0} = 0, \ x_{0,0,3} + x_{0,2,1} + x_{2,0,1} = 0, \end{array} \right\} \mathbf{D}$$

$$\kappa_{1,1} = \frac{1}{3} \left(x_{2,0,2} - x_{0,0,4} - 2x_{0,2,2} - x_{0,4,0} + x_{2,2,0} + 2x_{4,0,0} \right),$$

$$\kappa_{1,2} = x_{1,1,2} + x_{1,3,0} + x_{3,1,0}, \ \kappa_{1,3} = x_{1,0,3} + x_{1,2,1} + x_{3,0,1},$$

$$\kappa_{2,2} = \frac{1}{3} \left(x_{0,2,2} - x_{0,0,4} + 2x_{0,4,0} - 2x_{2,0,2} + x_{2,2,0} - x_{4,0,0} \right),$$

$$\kappa_{2,3} = x_{0,1,3} + x_{0,3,1} + x_{2,1,1}.$$
(B4)

subject to the "saddle" constraints (2D)

height $x_{0,2} + x_{2,0} = \nu, \ x_{1,2} + x_{3,0} = 0, \ x_{0,3} + x_{2,1} = 0, \ zero \ gradient$ $\kappa \cos(2\theta) = \frac{1}{2} (x_{4,0} - x_{0,4}), \ \kappa \sin(2\theta) = -x_{1,3} - x_{3,1}.$ Define the spin at point \mathbf{r}_y along the z direction as the anti-symmetric contraction of the de-traced tidal field and hessian: (2D)

$$L(\mathbf{r}_{y}) = \varepsilon_{ij} \overline{y}_{il} \overline{y}_{jmml} = (y_{2,0} - y_{0,2}) (y_{1,3} + y_{3,1}) + \frac{y_{1,1}}{2} (y_{0,4} - y_{4,0}) - \frac{y_{1,1}}{2} (y_{4,0} - y_{0,4}) .$$
(A3)

It is then fairly straightforward to compute the corresponding constrained expectation, $\langle L|pk\rangle$, for L as

$$L_{z}(r,\theta,\kappa,\nu) = \int L(\mathbf{Y}) PDF(\mathbf{X},\mathbf{Y}|pk) d\mathbf{X}d\mathbf{Y}.$$
 (A4)

e.g. for n=-2 Incredibly simple prediction !





e.g. for n=-2 **Incredibly simple prediction**!

$$(r^2-4)\cos(2\theta)+6$$
.

anti-ymmetry





In order to compute the spin distribution, the formalism developed in Section 2 is easily extended to 3D. A critical (including saddle condition) point constraint is imposed. The resulting mean density field subject to that constraint becomes (in units of σ_2):

$$\delta(\mathbf{r},\kappa,I_1,\nu|\text{ext}) = \frac{I_1(\xi_{\phi\delta}^{\Delta\Delta} + \gamma\xi_{\phi\phi}^{\Delta\Delta})}{1-\gamma^2} + \frac{\nu(\xi_{\phi\phi}^{\Delta\Delta} + \gamma\xi_{\phi\delta}^{\Delta\Delta})}{1-\gamma^2} + \frac{15}{2} \left(\mathbf{\hat{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \mathbf{\hat{r}}\right) \xi_{\phi\delta}^{\Delta+}, \quad (3.1)$$

where again $\overline{\mathbf{H}}$ is the detraced Hessian of the density and $\hat{\mathbf{r}} = \mathbf{r}/r$ and we define in 3D $\xi_{\phi x}^{\Delta +}$ as $\xi_{\phi \delta}^{\Delta +} = \langle \Delta \delta, \phi^+ \rangle$, with $\phi^+ = \phi_{11} - (\phi_{22} + \phi_{33})/2$. Note that $\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}$ is a scalar quantity defined explicitly as $\hat{r}_i \overline{H}_{ij} \hat{r}_j$. As in 2D, the expected spin can also be computed. In 3D, the spin is a vector, which components are given by $L_i = \varepsilon_{ijk} \delta_{kl} \phi_{lj}$, with $\boldsymbol{\epsilon}$ the rank 3 Levi Civita tensor. It is found to be orthogonal to the separation and can be written as the sum of two terms

$$\mathbf{L}(\mathbf{r},\kappa,I_1,\nu|\mathrm{ext}) = -15\left(\mathbf{L}^{(1)}(r) + \mathbf{L}^{(2)}(\mathbf{r})\right) \cdot \left(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \boldsymbol{\epsilon} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}\right),$$
(3.2)

where $\mathbf{L}^{(1)}$ depends on height, ν , and on the trace of the Hessian I_1 but not on orientation

$$\begin{split} \mathbf{L}^{(1)}(r) &= \left(\frac{\nu}{1-\gamma^2} \left[(\xi_{\phi\phi}^{\Delta+} + \gamma \xi_{\phi\delta}^{\Delta+}) \xi_{\delta\delta}^{\times\times} - (\xi_{\phi\delta}^{\Delta+} + \gamma \xi_{\delta\delta}^{\Delta+}) \xi_{\phi\delta}^{\times\times} \right] \\ &+ \frac{I_1}{1-\gamma^2} \left[(\xi_{\phi\delta}^{\Delta+} + \gamma \xi_{\phi\phi}^{\Delta+}) \xi_{\delta\delta}^{\times\times} - (\xi_{\delta\delta}^{\Delta+} + \gamma \xi_{\phi\delta}^{\Delta+}) \xi_{\phi\delta}^{\times\times} \right] \right) \mathbb{I}_3 \,, \end{split}$$

and $L^{(2)}(\mathbf{r})$ now depends on $\overline{\mathbf{H}}$ and on orientation:

$$\begin{split} \mathbf{L}^{(2)}(\mathbf{r}) &= -\frac{5}{8} \left[2((\xi_{\phi\delta}^{\Delta +} - \xi_{\phi\delta}^{\Delta \Delta})\xi_{\delta\delta}^{\times \times} - (\xi_{\delta\delta}^{\Delta +} - \xi_{\delta\delta}^{\Delta \Delta})\xi_{\phi\delta}^{\times \times}) \overline{\mathbf{H}} \right. \\ &+ ((7\xi_{\delta\delta}^{\Delta \Delta} + 5\xi_{\delta\delta}^{\Delta +})\xi_{\phi\delta}^{\times \times} - (7\xi_{\phi\delta}^{\Delta \Delta} + 5\xi_{\phi\delta}^{\Delta +})\xi_{\delta\delta}^{\times \times})(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}) \mathbb{I}_{3} \right] \,, \end{split}$$

3D Transition mass ?

Lagrangian theory capture spin flip !

Transition mass associated with **size** of quadrant





Geometry of the saddle provides **a natural 'metric'** (local frame as defined by Hessian @ saddle) relative to which **dynamical evolution** of DH is predicted.

cloud in cloud effect



Figure 5. Left: logarithmic cross section of $M_p(r, z)$ along the most likely (vertical) filament (in units of $10^{12} M_{\odot}$). Right: corresponding cross section of $\langle \cos \hat{\theta} \rangle(r, z)$. The mass of halos increases towards the nodes, while the spin flips.

geometric split — mass split

Geometry of the saddle provides a natural 'metric' (local frame as defined by Hessian @ saddle) relative to which dynamical evolution of DH is predicted.

cloud effect



Figure 6. Mean alignment between spin and filament as a function of mass for a filament smoothing scale of 5 Mpc/h. The spin flip transition mass is around $4 \, 10^{12} M_{\odot}$.

geometric split — mass split



Figure 5. top: Density caustic; Bottom: Zeldovitch mapping of the spin distribution



Back to wall winding : generation of vorticity

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X.



braids structure of vorticity.

Growth of large-scale structure



Vorticity generation



Alignment of vorticity with filaments

Vorticity is aligned with the filaments.



Filaments and walls are identified with DISPERSE: Sousbie+ (2011).

Geometry of the vorticity cross-section



Pichon & Bernardeau (1999)



Cross-sections are typically divided in 4 quadrants.

Theoretical prediction from Pichon & Bernardeau 1999

Low-mass halos are aligned with the filament



 Mhalo < Mcrit alignment of halo spin with filament increases with mass.

• Mcrit



High-mass halos are perpendicular



Mass dependent Halo spin - filament alignment



Halo-spin vorticity alignment vorticity along the filament



Geometry of the vorticity cross-section



High vorticity regions are located at the edges of the filament.

Idealized toy model: The position is fixed and the radius of the halo increases:



Transition mass is correlated with the size of the quadrants.

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in short...



Vorticity is confined in the filaments, and aligned with them. The cross-section with a plane perpendicular to the filament is typically quadripolar.





Halo spins are aligned with the same polarity than vorticity in quadrants.

Qualitatively, the transition mass in the alignment could be correlated with the size of the quadrant.



Explain transition mass? YES!



Explain transition mass? YES!








Take home message...

- Morphology (= AM stratification) driven by LSS in cosmic web: it explains Es & Sps where, how & why from ICs
- Signature in correlation between spin and internal kinematic structure of cosmic web on larger scales.
- Process driven by simple PBS/biassed clustering dynamics:
 - requires updating TTT to saddles: simple theory :-)
 - can be expressed into an Eulerian theory via vorticity

Where galaxies form does matter, and can be traced back to ICs Flattened filaments generate point-reflection-symmetric AM/vorticity distribution: they induce the observed spin transition mass

• which is why the δ -Web is the best :-)

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What about galaxies ??

Horizon-AGN simulation Jade (CINES)

- (PI Y. Dubois, Co-I J. Devriendt & C. Pichon)
- L_{box}=100 Mpc/h
- 1024³ DM particles $M_{DM,res}$ =8x10⁷ M_{sun}
- Finest cell resolution dx=1 kpc
- Gas cooling & UV background heating
- Low efficiency star formation
- Stellar winds + SNII + SNIa
- O, Fe, C, N, Si, Mg, H
- AGN feedback radio/quasar

Outputs

(backed up and analyzed on BEYOND)

- Simulation outputs
- Lightcones (1°x1°) performed on-the-fly
 - Dark Matter (position, velocity)
 - Gas (position, density, velocity, pressure, chemistry)
 - Stars (position, mass, velocity, age, chemistry)
 - Black holes (position, mass, velocity, accretion rate)

z=1.5 using 3 Mhours on 4096 cores

horizon-AGN.projet-horizon.fr

PART IV

z = 1.2

Part V Outline

Can morphology/physics trace spin flip?
Are transition masses consistent?
The fate of forming galaxies
The fate of merging galaxies

Galaxies versus dense filaments



Galaxies are strongly

clustered

near filaments

can morphology trace spin flip?

thanks to AGN feedback we have morphological diversity





Can morphological/physical properties of galaxies trace spin flip?



is morphometric transition mass consistent with DM ?

Final point 1/2: low mass galaxies

What is the *physical* origin of low mass **galaxies** spin-filament alignment ? Vorticity arising from kin. structure of filament!



Final point 2/2: high mass galaxies

What is the *physical* origin of spin flip? high mass **galaxies** merge!





Transition mass versus **merging rate** for galaxies



Caught in the rhythm: satellites in their galactic plane

C. Welker^{1*}, Y. Dubois¹, C. Pichon^{1,2}, J. Devriendt^{3,4} and N. E. Chisari³



Are the imprints of LSS noticeable on galaxy properties ?



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Summary of 1D Gaussian calculations



Maxima above threshold $\eta = \rho/\sigma_0$

$$n_{max}(\rho > \eta \sigma_0) = \begin{cases} n_{max} \mathcal{P}(\eta) & \gamma \to \mathbf{0} \\ n_{max} \mathcal{P}(\eta)(\gamma \eta) & \gamma \to \mathbf{1} \end{cases}$$

back to 2D Theory without Hessian approximation

